

NAG Toolbox for MATLAB

f11xe

1 Purpose

f11xe computes a matrix-vector product involving a real sparse symmetric matrix stored in symmetric co-ordinate storage format.

2 Syntax

```
[y, ifail] = f11xe(a, irow, icol, check, x, 'n', n, 'nnz', nnz)
```

3 Description

f11xe computes the matrix-vector product

$$y = Ax$$

where **a** is an **n** by **n** symmetric sparse matrix, of arbitrary sparsity pattern, stored in symmetric co-ordinate storage (SCS) format (see Section 2.1.2 in the F11 Chapter Introduction). The array **a** stores all nonzero elements in the lower triangular part of A , while arrays **irow** and **icol** store the corresponding row and column indices respectively.

It is envisaged that a common use of f11xe will be to compute the matrix-vector product required in the application of f11ge to sparse symmetric linear systems. An illustration of this usage appears in f11jd.

4 References

None.

5 Parameters

5.1 Compulsory Input Parameters

- 1: **a(nnz)** – double array

The nonzero elements in the lower triangular part of the matrix A , ordered by increasing row index, and by increasing column index within each row. Multiple entries for the same row and column indices are not permitted. The function f11zb may be used to order the elements in this way.

- 2: **irow(nnz)** – int32 array

- 3: **icol(nnz)** – int32 array

The row and column indices of the nonzero elements supplied in **a**.

Constraints:

$$1 \leq \mathbf{irow}(i) \leq \mathbf{n} \text{ and } 1 \leq \mathbf{icol}(i) \leq \mathbf{irow}(i), \text{ for } i = 1, 2, \dots, \mathbf{nnz};$$

$$\mathbf{irow}(i-1) < \mathbf{irow}(i) \quad \text{or} \quad \mathbf{irow}(i-1) = \mathbf{irow}(i) \quad \text{and} \quad \mathbf{icol}(i-1) < \mathbf{icol}(i), \quad \text{for } i = 2, 3, \dots, \mathbf{nnz}.$$

irow and **icol** must satisfy the following constraints (which may be imposed by a call to f11zb):

- 4: **check** – string

Specifies whether or not the input data should be checked.

check = 'C'

Checks are carried out on the values of **n**, **nnz**, **irow** and **icol**.

check = 'N'

None of these checks are carried out.

See also Section 8.2.

Constraint: **check** = 'C' or 'N'.

5: **x(n)** – **double array**

The vector x .

5.2 Optional Input Parameters

1: **n** – **int32 scalar**

Default: The dimension of the arrays **x**, **y**. (An error is raised if these dimensions are not equal.)
 n , the order of the matrix A .

Constraint: $n \geq 1$.

2: **nnz** – **int32 scalar**

Default: The dimension of the arrays **a**, **irow**, **icol**. (An error is raised if these dimensions are not equal.)

the number of nonzero elements in the lower triangular part of A .

Constraint: $1 \leq \text{nnz} \leq n \times (n + 1)/2$.

5.3 Input Parameters Omitted from the MATLAB Interface

None.

5.4 Output Parameters

1: **y(n)** – **double array**

The vector y .

2: **ifail** – **int32 scalar**

0 unless the function detects an error (see Section 6).

6 Error Indicators and Warnings

Errors or warnings detected by the function:

ifail = 1

On entry, **check** $\neq$ 'C' or 'N'.

ifail = 2

On entry, $n < 1$,
 or $\text{nnz} < 1$,
 or $\text{nnz} > n \times (n + 1)/2$.

ifail = 3

On entry, the arrays **irow** and **icol** fail to satisfy the following constraints:

$1 \leq \mathbf{irow}(i) \leq \mathbf{n}$ and $1 \leq \mathbf{icol}(i) \leq \mathbf{irow}(i)$, for $i = 1, 2, \dots, \mathbf{nnz}$;

$\mathbf{irow}(i-1) < \mathbf{irow}(i)$, or $\mathbf{irow}(i-1) = \mathbf{irow}(i)$ and $\mathbf{icol}(i-1) < \mathbf{icol}(i)$, for $i = 2, 3, \dots, \mathbf{nnz}$.

Therefore a nonzero element has been supplied which does not lie in the lower triangular part of A , is out of order, or has duplicate row and column indices. Call `f11zb` to reorder and sum or remove duplicates.

7 Accuracy

The computed vector y satisfies the error bound

$$\|y - Ax\|_{\infty} \leq c(n)\epsilon\|A\|_{\infty}\|x\|_{\infty},$$

where $c(n)$ is a modest linear function of n , and ϵ is the *machine precision*.

8 Further Comments

8.1 Timing

The time taken for a call to `f11xe` is proportional to $\mathbf{nnz}$.

8.2 Use of check

It is expected that a common use of `f11xe` will be to compute the matrix-vector product required in the application of `f11ge` to sparse symmetric linear systems. In this situation `f11xe` is likely to be called many times with the same matrix A . In the interests of both reliability and efficiency you are recommended to set **check** to 'C' for the first of such calls, and to 'N' for all subsequent calls.

9 Example

```
a = [4;
     -1;
      6;
      1;
      2;
      3;
      2;
      4;
      1;
      2;
      6;
     -4;
      1;
     -1;
      6;
     -1;
     -1;
      3;
      1;
      1;
     -1;
      1;
      4];
irow = [int32(1);
        int32(2);
        int32(2);
        int32(3);
        int32(3);
        int32(4);
        int32(5);
        int32(5);
        int32(6);
```

```

        int32(6);
        int32(6);
        int32(7);
        int32(7);
        int32(7);
        int32(7);
        int32(8);
        int32(8);
        int32(8);
        int32(9);
        int32(9);
        int32(9);
        int32(9);
        int32(9)];
icol = [int32(1);
        int32(1);
        int32(2);
        int32(2);
        int32(3);
        int32(4);
        int32(1);
        int32(5);
        int32(3);
        int32(4);
        int32(6);
        int32(2);
        int32(5);
        int32(6);
        int32(7);
        int32(4);
        int32(6);
        int32(8);
        int32(1);
        int32(5);
        int32(6);
        int32(8);
        int32(9)];
check = 'C';
x = [0.7;
      0.16;
      0.52;
      0.77;
      0.28;
      0.21;
      0.93;
      0.2;
      0.9];
[y, ifail] = f11xe(a, irow, icol, check, x)

```

```

y =
    4.1000
   -2.9400
    1.4100
    2.5300
    4.3500
    1.2900
    5.0100
    0.5200
    4.5700
ifail =
      0

```